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15. May 2009

Online at <http://mpra.ub.uni-muenchen.de/15264/>

MPRA Paper No. 15264, posted 17. May 2009 00:29 UTC

Algorithm for payoff calculation for option trading strategies using vector terminology

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Abstract

The aim of this paper is to develop an algorithm for calculating and plotting payoff of option strategies for a portfolio of path independent vanilla and exotic options. A general algorithm for calculating the vector matrix for any arbitrary combination strategy is also developed for some of the commonly option trading strategies.

1.0 Introduction

Hull [1] discusses the payoffs for long and short positions in Call and Put options by using algebraic techniques. J.S. Chaput & L.H. Ederington [3] , Natenberg[2] and Hull[1] contain the bibliographies and survey of literature on the theoretical background of option strategies for path independent vanilla and exotic options such as European , Bermuda , Forward Start , Digital/Binary and Quanto options. There are various open source option strategy calculators like “Option” [4] that only rely on algebraic analytical and graph superposition techniques to plot graphs for overall profit/loss. We in this paper develop an algorithm using vector terminology to plot final profit/loss graph of various option strategies.

2.1 Option strategies using vector notation

For a spot price S_T at time T and a strike price K , the payoff for a long position in call option is given by $\text{Max}(S_T - K, 0)$ and the payoff is $\text{Min}(S_T - K, 0)$ for the short position in the call option. Similarly the payoff for a long position in put is $\text{Max}(K - S_T, 0)$ whereas it is $\text{Min}(S_T - K, 0)$ for a short position in the put option. We can represent a vector payoff matrix for any option strategy as a $2 \times N$ matrix.

Vector	V_1	V_2	V_n
Strike Price	K_1	K_2	K_n

In the above matrix the strike prices K_1, K_2, \dots, K_n for combination of options are in the ascending order, i.e., $K_1 < K_2 < \dots < K_n$. The vector V_i can be interpreted as slope of the payoff graph of option strategy. By default the smallest strike price is always taken to be zero i.e. $K_1 = 0$. The vector is always an integer in the interval $(-\infty, \infty)$. We can interpret the above matrix in terms of slope of the profit/loss curve obtained for option strategies.

$$\text{slope} = \begin{cases} V_i, & \text{for } K_i < K < K_{i+1} \text{ and } i < n \\ V_i, & \text{for } K > K_n \text{ and } i = n \end{cases}$$

Vector matrix for long and short position is given by

Long Position				Short Position			
V_1	V_2	V_n	$-V_1$	$-V_2$	$-V_n$
K_1	K_2	K_n	K_1	K_2	K_n

Using the above vector notation we can represent long and short position in call option as under

Long call		Short Call	
0	+1	0	-1
0	K_1	0	K_1

For long position in call, profit/loss curve has two slopes 0 and +1 whereas for a short position the slope of profit/loss curve has two slopes 0 and -1.

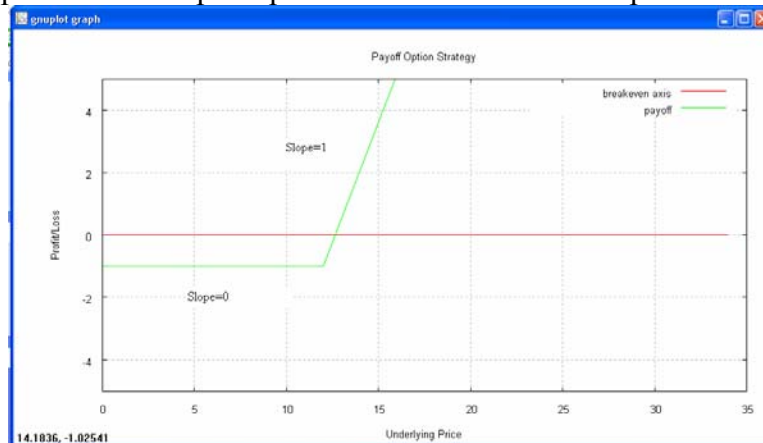


Figure1: Long Position in Call Option

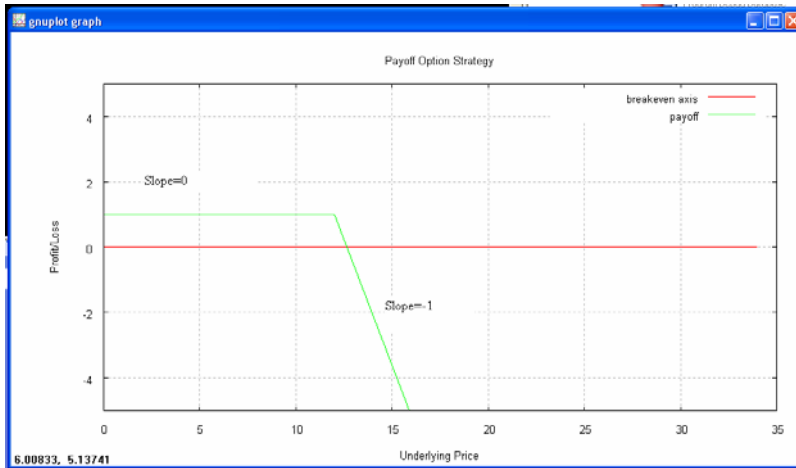


Figure 2: Short position in Call Option

Similarly, the vector matrix for long and short position in put options are:

Long Put	
-1	0
0	K_1

Short Put	
+1	0
0	K_1

For long position in stock, the slope of profit/loss curve is +1 and strike price is assumed to be zero whereas for short position in stock, the slope of profit/loss curve is -1 and strike price is assumed to be zero. The vector matrix notation is given as:

Long Stock	
+1	
0	

Short Stock	
-1	
0	

When we trade in n units of options using a particular option strategy, the entire vector row is multiplied by n .

$n \cdot V_1$	$n \cdot V_2$	$n \cdot V_n$
K_1	K_2	K_n

The data set for a portfolio using n option strategies can be represented as

Strategy 1

V_{11}	V_{12}
K_{11}	K_{12}

Strategy 2

V_{21}	V_{22}
K_{21}	K_{22}

...

...

...

Strategy i

V_{i1}	V_{i2}	V_{ij}
K_{i1}	K_{i2}	K_{ij}

....

....

....

Strategy n

V_{n1}	V_{n2}	...	V_{nm}
K_{n1}	K_{n2}	K_{nm}

Note that the number of columns in each option strategy can be different. We can use the above derived vector matrices to form profit/loss function for any combination of option strategies using the following algorithm:

Algorithm

To plot the overall payoff strategy we need the initial Y intercept of the strategy apart from the resultant vector matrix. This Y intercept can be calculated using matrices of length greater than one using the formula

```
Yint =  $\sum$  ( -1*Vector(A[j])*Strike_price(A[j+1]) )
Yint = Yint + Net_Premium_Paid
```

Step 1

```
For I  $\leftarrow$  1 to no_of_options
    For j  $\leftarrow$  1 to length_of_option_matrix
        Insert A[j] in Result_matrix in sorted increasing order on
        the basis of Strike_price(A[j]).
```

Step 2

```
For k  $\leftarrow$  1 to length_of_Result_matrix
    Vector(B[k])=0
    For I  $\leftarrow$  1 to no_of_options
        For j  $\leftarrow$  1 to length_of_option_matrix
            If Strike_price(B[k]) = Strike_price(A[j])
                Vector(B[k]) = Vector(B[k])+ Vector(A[j])
            ElseIf j < length_of_option_matrix
                If Strike_price(A[j]) < Strike_price(B[k]) <
                Strike_price(A[j+1])
                    Vector(B[k]) = Vector(B[k])+ Vector(A[j])
            Else
                Vector(B[k]) = Vector(B[k])+ Vector(A[j])
```

Step 3

```
For I  $\leftarrow$  1 to no_of_options
    j=1
    If length_of_option_matrix > 1
        Yint = Yint + -1 * Vector(A[j]) * Strike_price(A[j+1])
Yint = Yint + NetPremium
```

Step 4

```
For k  $\leftarrow$  1 to length_of_Result_matrix - 1
    Plot line with slope Vector(B[k]) & Y Intercept Yint
    between points Strike_price(B[k]) & Strike_price(B[k+1])
    ypoint=Vector(B[k])*( Strike_price(B[k+1]) - Strike_price(B[k]) )
    + Yint
    Yint = ypoint - Vector(B[k+1])* Strike_price(B[k+1])
k = length_of_Result_matrix
Plot line with slope Vector(B[k]) between points Strike_price(B[k]) &
infinity
```

The source code for the above algorithm is written and implemented on VC++.Net 2005 using open source graph plotting utility Gnuplot.

Illustration 1: An investor buys \$3 put with strike price \$35 and sells for \$1 a put with a strike price of \$30.

(Example 10.2, page 224 given in Hull [1])

The above data can be represented as

Buy Put		+	Sell Put		=	Payoff(Bear Spread)		
-1	0		+1	0		0	-1	0
0	35		0	30		0	30	35

Initial Y intercept is $-1*(-1*35) + -1*(1*30) - 3 + 1 = 35 - 30 - 3 + 1 = 3$

One can use the following form to input the data of his/her option strategy:

The screenshot shows a window titled "Form1" with a blue border. Inside, there are several radio buttons for selecting an option strategy: "BuyStock", "SellStock", "Buy Call Option", "Sell Call Option", "Buy Put Option" (which is selected with a green dot), and "Sell Put Option". To the right of these are input fields for "No Of Units" (value: 1), "Stock Price" (value: 0.0), "Strike Price" (value: 35), and "Premium" (value: 3). Below the radio buttons are two buttons: "Add To Portfolio" and "Plot". At the bottom, there is a "Profit/Loss at Price" input field (value: 0.0) and a "Show PayOff" button.

Figure 3: Input Screen

The following is the output of the final payoff of combination of option strategy in vector notation as discussed above.

The screenshot shows a small dialog box with a blue title bar and a red close button. The text inside reads "Vector PayOffMatrix" followed by a 2x3 matrix of values: 0, -1, 0 in the first row and 0, 30, 35 in the second row. Below the matrix is an "OK" button.

Figure 4: Vector Payoff Matrix

The algorithm gives the following resultant profit/loss graph of the above combination of option strategies in the form of a bear put spread.

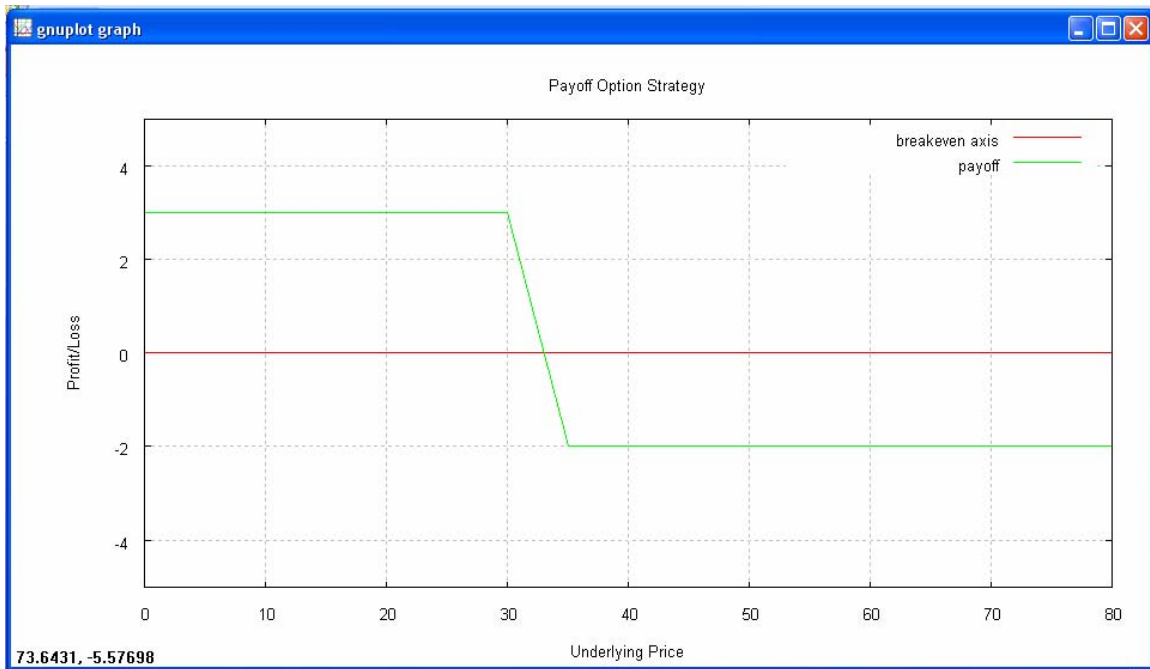


Figure 5: Payoff Graph

The loss is \$2 if stock price is above \$35 and the profit is \$3 if stock price below \$30.

2.2 Some More Complex Strategies

The following are the vector matrices for some of the commonly traded strategies:

Long Combo

$(0 < K_1 < K_2)$

Sell Put

+1	0
0	K_1

+

Buy Call

0	+1
0	K_2

=

Long Combo

+1	0	+1
0	K_1	K_2

Long Straddle

Buy Put

-1	0
0	K_1

+

Buy Call

0	+1
0	K_1

=

Long Straddle

-1	+1
0	K_1

Short Straddle

The vector matrix of short straddle is negative of that of long straddle

+1	-1
0	K_1

<u>Strip</u> Buy call		+	Buy 2 puts		=	Strip	
0	+1		-2	0		-2	+1
0	K_1		0	K_1		0	K_1

<u>Strap</u> Buy 2 calls		+	Buy put		=	Strap	
0	+2		-1	0		-1	+2
0	K_1		0	K_1		0	K_1

<u>Long Strangle</u> ($0 < K_1 < K_2$) Buy put		+	Buy call		=	Long Strangle		
-1	0		0	+1		-1	0	+1
0	K_1		0	K_2		0	K_1	K_2

Short Strangle
The vector matrix of short strangle is negative of that of short strangle. ($0 < K_1 < K_2$)

+1	0	-1
0	K_1	K_2

<u>Collar</u> ($0 < K_1 < K_2$) Long Stock		+	Buy Put		+	Sell call		=
+1			-1	0		0	-1	
0			0	K_1		0	K_2	
Collar								
0	+1	0						
0	K_1	K_2						

<u>Box Spread</u> ($0 < K_1 < K_2$) Buy Call		+	Sell call		+	Sell Put		+	Buy Put		=
0	+1		0	-1		+1	0		-1	0	
0	K_1		0	K_2		0	K_1		0	K_2	
Box Spread											
0	0	0									
0	K_1	K_2									

<u>Long Call Butterfly</u> ($0 < K_1 < K_2 < K_3$) Buy Call		+	Sell 2 call		+	Buy Call		=
0	+1		0	-2		0	+1	
0	K_1		0	K_2		0	K_3	
Long Call Butterfly								
0	+1	-1	0					
0	K_1	K_2	K_3					

Short Call Butterfly

The vector matrix of short call butterfly is negative of that of long call butterfly ($0 < K_1 < K_2 < K_3$)

0	-1	+1	0
0	K_1	K_2	K_3

Long Call Condor

($0 < K_1 < K_2 < K_3 < K_4$)

Buy Call		+	Sell call		+	Sell Call		+	Buy Call	
0	+1		0	-1		0	-1		0	+1
0	K_1		0	K_2		0	K_3		0	K_4

Long Call Condor

0	+1	0	-1	0
0	K_1	K_2	K_3	K_4

Short Call Condor

The vector matrix of short call condor is negative of that of long call condor ($0 < K_1 < K_2 < K_3 < K_4$)

0	-1	0	+1	0
0	K_1	K_2	K_3	K_4

Illustration 2: Let a certain stock is selling at \$77. An investor feels that significant change in price is un-likely in the next 3 months. He observes market price of 3 month calls as

Strike Price(\$)	Call Price(\$)
75	12
80	8
85	5

The investor decided to go long in two calls each with strike price \$75 and \$85 and writes two calls with strike price \$80. Payoff for different levels of stock prices is given as

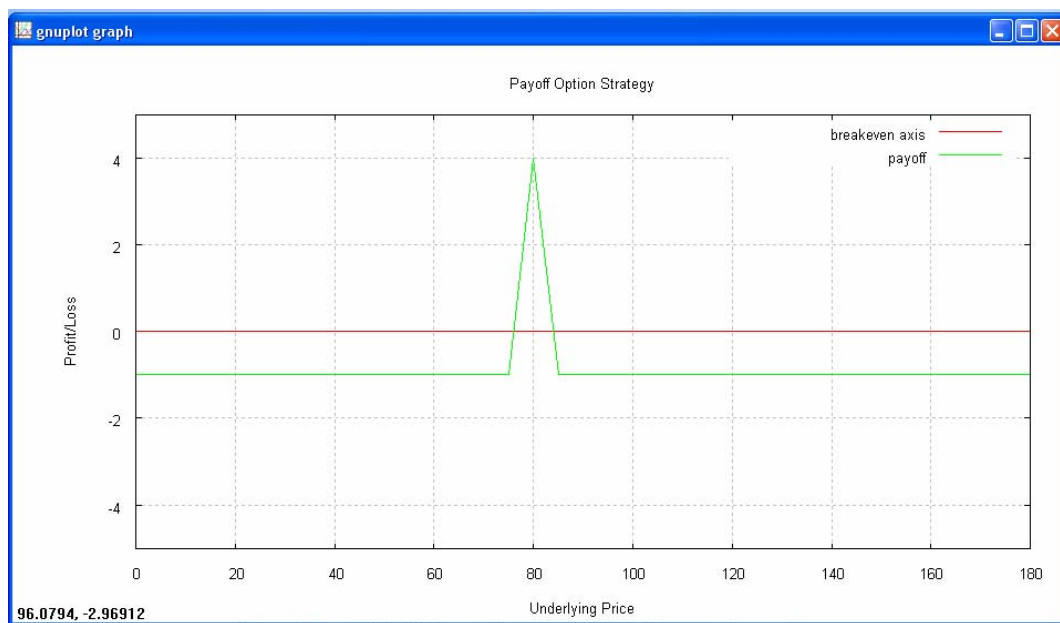


Figure 6: Payoff Graph

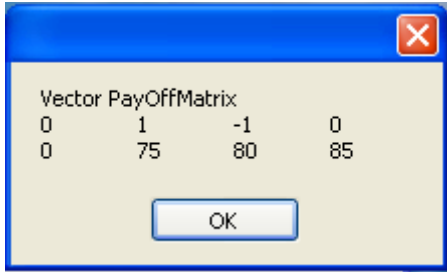


Figure 7: Vector Payoff Matrix

The profit /loss when stock price is at maturity is

Stock Price(\$)	Profit/Loss(\$)
65	-1
68	-1
73	-1
78	2
83	1

References

- [1] Hull, J.C.(2009) *Options, Futures, and Other Derivatives* ,Prentice Hall .
- [2] Natenberg,S.(1994) *Option Volatility and Pricing Strategies: Advanced Trading Techniques for Professionals* McGraw-Hill Professional Publishing .
- [3] Chaput, J. S. and Ederington L. H., “Option Spread and Combination Trading” *Journal of Derivatives*, 10, 4(Summer 2003):70-88.
- [4] <http://sourceforge.net/projects/option>